Haskell Answers 7: Tuples

Antoni Diller

4 August 2011

(1) An association list is a list of 2-tuples. For example, [("temp", 34), ("height", 80), ("weight", 180), ("depth", 7)]. Define a function $domain :: Eq \ a \Rightarrow [(a,b)] \rightarrow [a]$ which takes an association list and returns the list of all those things that occur in the first component of each tuple. Make sure that the value of domain does not contain any duplicates.

```
nub :: Eq a => [a] -> [a]
nub = nubBy (==)

nubBy :: (a -> a -> Bool) -> [a] -> [a]
nubBy eq [] = []
nubBy eq (x:xs) = x : nubBy eq (filter (\y -> not (eq x y)) xs)

domain :: Eq a => [(a, b)] -> [a]
domain ass = nub [x | (x, _) <- ass]</pre>
```

(2) Define a function $range :: Eq \ a \Rightarrow [(a,b)] \rightarrow [b]$ which takes an association list and returns the list of all those things that occur in the second component of each tuple. Make sure that the value of range does not contain any duplicates.

```
range1 :: Eq b => [(a, b)] -> [b]
range1 ass = nub [y | (_, y) <- ass]
```

(3) Define a function $compose :: [(a,b)] \to [(b,c)] \to [(a,c)]$ such that a tuple (x,z) is in the list returned as the value of the function $compose \ ass1 \ ass2$ iff (x,y) is in $ass1 \ and \ (y,z)$ is in ass2. For example, compose [(1, 2), (7, 11)] [(2, 3), (11, 14)] is [(1, 3), (7, 14)].

```
compose :: [(a, b)] \rightarrow [(b, c)] \rightarrow [(a, c)]
compose ass1 ass2 = [(x, z) \mid (x, y) \leftarrow ass1, (y, z) \leftarrow ass2]
```

(4) Define a function *inverse* :: $[(a,b)] \rightarrow [(b,a)]$ such that a tuple (y,x) is in *inverse ass* iff (x,y) is in ass.

```
inverse :: [(a, b)] \rightarrow [(b, a)]
inverse ass = [(y, x) \mid (x, y) \leftarrow ass]
```

(5) A homogeneous association list is one whose tuples contain elements belonging to the same type. Define a function reflexive :: $Eq\ a \Rightarrow [(a,a)] \rightarrow Bool$ which tests to see if a homogeneous association list is reflexive, that is to say, if either (x,y) or (y,x) is in ass, then (x,x) is also in ass.

```
member x [] = False
member x (y:ys)
    | x == y = True
    | otherwise = member x ys
reflexive :: Eq a => [(a, a)] -> Bool
reflexive ass =
    and [member (x, x) ass | x <- (domain ass) ++ (range1 ass)]</pre>
```

(6) Define a function symmetric :: Eq $a \Rightarrow [(a,a)] \rightarrow Bool$ which tests to see if a homogeneous association list is symmetric, that is to say, if (x,y) is in ass, then so is (y,x).

```
symmetric :: Eq a => [(a, a)] -> Bool
symmetric ass = and [member (y, x) ass | (x, y) <- ass]
```

(7) Define a function transitive :: $Eq\ a \Rightarrow [(a,a)] \rightarrow Bool$ which tests to see if a homogeneous association list ass is transitive, that is to say, if (x,y) and (y,z) are in ass, then so is (x,z).

```
transitive :: Eq a => [(a, a)] -> Bool
transitive ass =
and [member (x, z) ass | (x, y) <- ass, (y, z) <- ass]
```

- (8) Define a function $closure :: [(a, a)] \to [(a, a)]$ which takes an arbitrary association list ass and produces the reflexive, transitive closure of ass, that is to say, if (x, y) and (y, z) are in ass, then (x, y), (y, z) and (x, z) are all in closure ass.
- (9) Define the function pairs such that pairs i is the list of all distinct pairs of integers

(x,y) such that $1 \le x, y \le i$. For example,

pairs
$$3 = [(1, 2), (1, 3), (2, 1), (2, 3), (3, 1), (3, 2)].$$

```
pairs :: Integral a => a -> [(a,a)]
pairs i = [ (x,y) | x <- [1..i], y <- [1..i], x /= y ]</pre>
```

- (10) Using the function zip define the infinite list factlist of factorials.
- (11) A curried function f of n Boolean arguments is called tautologous if it returns True for every one of the 2^n possible combinations of Boolean arguments. Write a function taut so that taut n f is True is and only if f is tautologous.